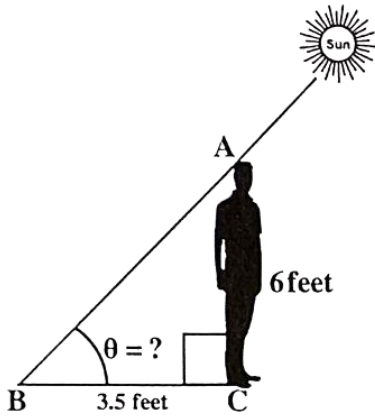


EXERCISE 7.5

Q.1. Find the angle of elevation of the sun if a 6 feet man casts a 3.5 feet shadow.

Solution:



From the figure we observe that

$$\text{Height of man} = m\overline{AC} = 6 \text{ feet}$$

$$\text{Length of shadow} = m\overline{BC} = 3.5 \text{ feet}$$

$$\text{Angle of elevation} = \theta = ?$$

Using the fact that

$$\tan \theta = \frac{m\overline{AC}}{m\overline{BC}}$$

$$\tan \theta = \frac{6}{3.5}$$

$$\theta = \tan^{-1} \frac{6}{3.5}$$

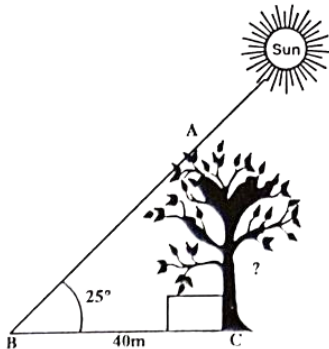
$$\theta = 59.7436$$

$$\theta = 59.74^\circ$$

So, the angle of elevation is $59^\circ 44'37''$.

Q.2. A tree casts a 40 meters shadow when the angle of elevation of the sun is 25° . Find the height of the tree.

Solution:



From the figure

$$\text{Height of tree} = m\overline{AC} = ?$$

$$\text{Length of shadow} = m\overline{BC} = 40\text{m}$$

$$\text{Angle of elevation} = \theta = 25^\circ$$

Using the fact that

$$\tan \theta = \frac{m\overline{AC}}{m\overline{BC}}$$

$$\tan 25^\circ = \frac{m\overline{AC}}{40}$$

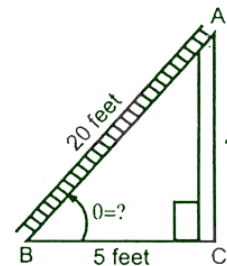
$$m\overline{AC} = 40 \times \tan 25^\circ$$

$$m\overline{AC} = 18.65 \text{ m}$$

So, height of tree is 18.65 m

Q.3. A 20 feet long ladder is leaning against a wall. The bottom of the ladder is 5 feet from the base of the wall. Find the acute angle (angle of elevation) the ladder makes with the ground.

Solution:



From the figure

$$\text{Length of ladder} = m\overline{AB} = 20 \text{ feet}$$

$$\text{Distance of ladder from the wall} = m\overline{BC} = 5 \text{ feet}$$

$$\text{Angle of elevation} = \theta = ?$$

Using the fact that

$$\cos \theta = \frac{m\overline{BC}}{m\overline{AB}}$$

$$\cos \theta = \frac{5 \text{ ft.}}{20 \text{ ft.}}$$

$$\cos \theta = 0.25$$

$$\theta = \cos^{-1}(0.25)$$

$$\theta = 75.5225$$

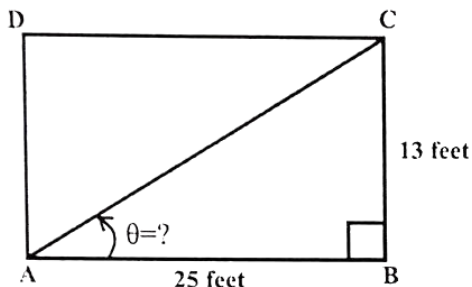
$$\theta = 75.5^\circ$$

or $\theta = 75^\circ 30'$

So, angle of elevation is $75^\circ 31'21''$

Q.4. The base of rectangle is 25 feet and the height of rectangle is 13 feet. Find the angle that the diagonal of the rectangle makes with the base.

Solution:



From the figure

Base of rectangle = $m\overline{AB} = 25$ feet

Height of rectangle = $m\overline{BC} = 13$ feet

Diagonal \overline{AC} is taken

Angle between diagonal and base = $\theta = ?$

Using the fact that

$$\tan\theta = \frac{m\overline{BC}}{m\overline{AB}}$$

$$\tan\theta = \frac{13}{25}$$

$$\theta = \tan^{-1} \frac{13}{25}$$

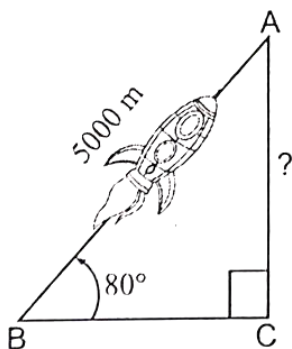
$$\theta = 27.4744$$

$$\theta = 27.47^\circ$$

So, angle between diagonal and base is $27^\circ 28' 28''$.

Q.5. A rocket is launched and climbs at a constant angle of 80° . Find the altitude of the rocket after it travels 5000 meter.

Solution:



From the figure

Distance travelled by rocket = $m\overline{AB} = 5000$ m

Altitude of rocket = $m\overline{AC} = ?$

Angle of elevation = $\theta = 80^\circ$

Using $\sin\theta = \frac{m\overline{AC}}{m\overline{AB}}$

$$\sin 80^\circ = \frac{m\overline{AC}}{5000}$$

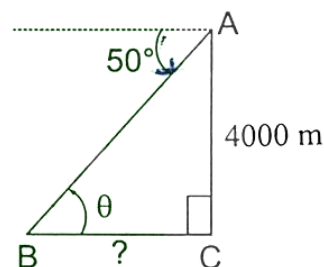
$$m\overline{AC} = 5000 \times \sin 80^\circ$$

$$m\overline{AC} = 4924.04$$

So, the altitude of rocket is 4924.04m

Q.6. An aeroplane pilot flying at an altitude of 4000m wishes to make an approach to an airport at an angle of 50° with the horizontal. How far from the airport will the plane be when the pilot begins to descend?

Solution:



From the figure

Altitude of aeroplane = $m\overline{AC} = 4000$ m

Distance of plane from airport = $m\overline{BC} = ?$

Angle of depression = 50°

As the alternate angles of parallel lines are equal, so angle

$$\theta = 50^\circ$$

Using the fact that, $\tan\theta = \frac{m\overline{AC}}{m\overline{BC}}$

$$\tan 50^\circ = \frac{4000}{m\overline{BC}}$$

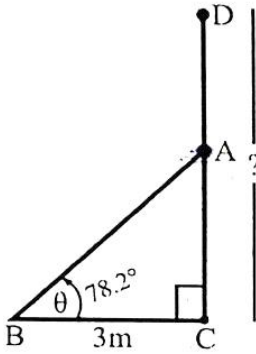
$$m\overline{BC} = \frac{4000}{\tan 50^\circ}$$

$$m\overline{BC} = 3356.4$$

So, the distance of aeroplane from airport is 3356.4 m.

Q.7. A guy wire (supporting wire) runs from the middle of a utility pole to the ground. The wire makes an angle of 78.2° with the ground and touch the ground 3 meters from the base of the pole. Find the height of the pole.

Solution:



From the figure

Height of pole = $m\overline{CD}$? =

Distance of wire from the base of the pole
= $m\overline{BC}$ = 3m

Angle of elevation = $\theta = 78.2^\circ$

As the wire is attached with the pole at its middle point A, so, first we find $m\overline{AC}$

Using the fact that

$$\tan \theta = \frac{m\overline{AC}}{m\overline{BC}}$$

$$\tan 78.2 = \frac{m\overline{AC}}{3}$$

$$m\overline{AC} = 3m \times \tan 78.2^\circ$$

$$m\overline{AC} = 14.36 \text{ m}$$

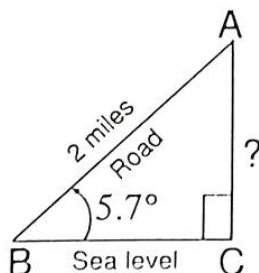
So Height of pole is = $m\overline{DC} = 2(m\overline{AC})$

$$= 2 \times 14.36 \text{ m}$$

$$= 28.72 \text{ m}$$

Q.8. A road is inclined at an angle 5.7° . Suppose that we drive 2 miles up this road starting from sea level. How high above sea level are we?

Solution:



From the figure

Distance covered on road = $m\overline{AB} = 2$ miles

Angle of inclination = $\theta = 5.7^\circ$

Height from sea level = $m\overline{AC}$? =

Using the fact that,

$$\sin \theta = \frac{m\overline{AC}}{m\overline{AB}}$$

$$\sin 5.7^\circ = \frac{m\overline{AC}}{2}$$

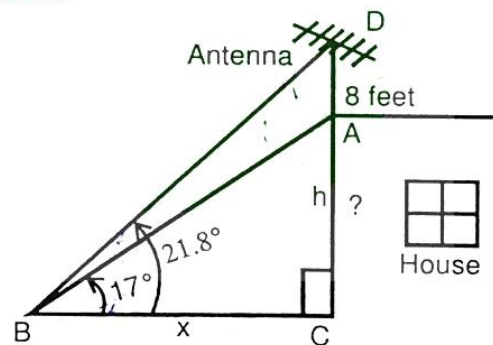
$$m\overline{AC} = 2 \times \sin 5.7^\circ$$

$$m\overline{AC} = 0.199 \text{ mile}$$

Hence, we are at the height of 0.199 mile from the sea level.

Q.9. A television antenna of 8 feet height is located on the top of a house. From a point on the ground the angle of elevation to the top of the house is 17° and the angle of elevation to the top of antenna is 21.8° . Find the height of the house.

Solution:



From the figure

Distance of point from house = $m\overline{BC} = x$

Height of house = $m\overline{AC} = h$?

Height of antenna = $m\overline{AD} = 8$ feet

Angle of elevation of top of house = 17°

Angle of elevation of top of antenna = 21.8°

In right angled ΔABC

$$\tan 17^\circ = \frac{m\overline{AC}}{m\overline{BC}}$$

$$\tan 17^\circ = \frac{h}{x}$$

$$x = \frac{1}{\tan 17^\circ} \times h$$

$$x = 3.271 \times h \dots\dots(i)$$

Now in right angle $\triangle DBC$

$$\tan 21.8 = \frac{\overline{mCD}}{\overline{mBC}}$$

$$\tan 21.8 = \frac{\overline{mAD} + \overline{mAC}}{\overline{mBC}}$$

$$\tan 21.8 = \frac{8+h}{x}$$

$$0.40 = \frac{8+h}{3.271h} \quad [\text{From (i)}]$$

$$0.40 \times 3.271h = 8 + h$$

$$1.3084 h - h = 8$$

$$(1.3084 - 1) h = 8$$

$$0.3084 h = 8$$

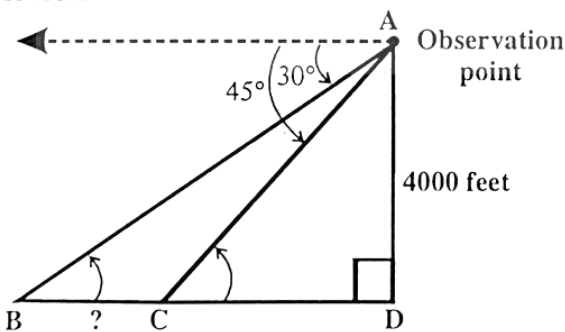
$$h = \frac{8}{0.3084}$$

$$h = 25.94 \text{ feet}$$

So, the height of the house is 25.94 feet

Q.10. From an observation point, the angles of depression of two boats in line with this point are found to 30° and 45° . Find the distance between the two boats if the point of observation is 4000 feet high.

Solution:



From the figure

Height of observation point = $\overline{mAD} = 4000$ feet

Distance between boats = $\overline{mBC} = ?$

Angles of depression of points B and C are 30° and 45° respectively from point A.

As the alternate angles of parallel lines are equal, so

$$m\angle B = 30^\circ \text{ and } m\angle C = 45^\circ$$

Now in right angled $\triangle ACD$

$$\tan 45^\circ = \frac{\overline{mAD}}{\overline{mCD}}$$

$$1 = \frac{4000}{\overline{mCD}}$$

$$\overline{mCD} = 4000 \text{ feet}$$

Now in right angled $\triangle BCD$

$$\tan 30^\circ = \frac{\overline{mAD}}{\overline{mBD}}$$

$$\frac{1}{\sqrt{3}} = \frac{4000}{\overline{mBC} + \overline{mCD}}$$

$$\frac{1}{\sqrt{3}} = \frac{4000}{\overline{mBC} + 4000}$$

$$\overline{mBC} + 4000 = 4000\sqrt{3}$$

$$\overline{mBC} = 4000\sqrt{3} - 4000$$

$$\overline{mBC} = 6928.20 - 4000$$

$$\overline{mBC} = 2928.20 \text{ feet}$$

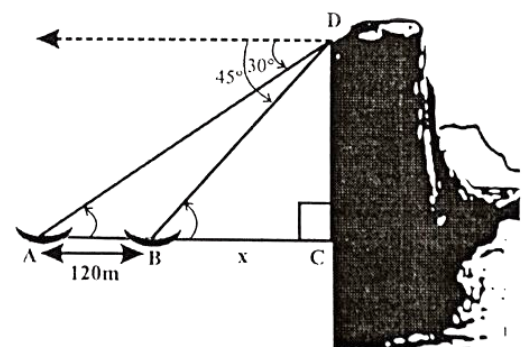
So, the distance between boats is 2928.2 feet.

Q.11. Two ships, which are in line with the base of a vertical cliff are 120 meters apart. The angles of depression from the top of the cliff to the ships are 30° and 45° , as shown in the diagram.

(a) Calculate the distance BC

(b) Calculate the height CD of the cliff.

Solution:



From the figure

Height of cliff = $\overline{CD} = h = ?$

Distance = $\overline{BC} = x = ?$

Distance between boats = $\overline{AB} = 120$ m

Angles of depression from point D to points A and B are 30° and 45° respectively.

As the alternate angles of parallel lines are equal, so $m\angle A = 30^\circ$ and $m\angle B = 45^\circ$

In right angled $\triangle ABCD$

$$\tan 45^\circ = \frac{m\overline{CD}}{m\overline{BC}}$$

$$1 = \frac{h}{x}$$

$$x = h \quad \dots\dots (i)$$

Now in right angled $\triangle ACD$

$$\tan 30^\circ = \frac{m\overline{CD}}{m\overline{AC}}$$

$$\frac{1}{\sqrt{3}} = \frac{h}{m\overline{AB} + m\overline{BC}}$$

$$\frac{1}{\sqrt{3}} = \frac{h}{120 + x}$$

$$120 + x = \sqrt{3} h$$

$$120 + h = \sqrt{3} h \quad (x = h)$$

$$120 = \sqrt{3} h - h$$

$$120 = (\sqrt{3} - 1)h$$

$$120 = (1.7321 - 1)h$$

$$120 = 0.7321 h$$

$$\frac{120}{0.7321} = h$$

$$h = 163.91 \text{ m}$$

As $x = h$, so

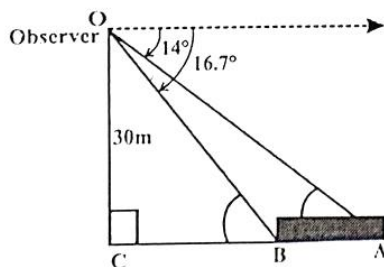
$$x = 163.91 \text{ m or } \underline{164 \text{ m}}$$

Thus Distance $m\overline{BC} = 164 \text{ m}$

Height of cliff $= m\overline{CD} = 164 \text{ m}$

Q.12. Suppose that we are standing on a bridge 30 meter above a river watching a log (piece of wood) floating towards us. If the angle with the horizontal to the front of the log is 16.7° and angle with the horizontal to the back of the log is 14° , how long is the log?

Solution:



From the figure

Height of observer's position $= m\overline{OC} = 30 \text{ m}$

Length of log of wood $= m\overline{AB} = x = ?$

Angles of depression from point O of the points A and B are 14° and 16.7° respectively.

In right angled $\triangle OBC$

$$\tan 16.7^\circ = \frac{m\overline{OC}}{m\overline{BC}}$$

$$0.30 = \frac{30}{m\overline{BC}}$$

$$m\overline{BC} = \frac{30}{0.30}$$

$$m\overline{BC} = 100 \text{ m}$$

Now in right angled $\triangle OAC$

$$\tan 14^\circ = \frac{m\overline{OC}}{m\overline{AC}}$$

$$0.249 = \frac{30}{m\overline{AB} + m\overline{BC}}$$

$$0.249 = \frac{30}{(x + 100)}$$

$$0.249(x + 100) = 30$$

$$x + 100 = \frac{30}{0.249}$$

$$x + 100 = 120.482$$

$$x = 120.482 - 100$$

$$x = 20.482 \text{ m}$$

So the length of log is 20.482 m.