

## EXERCISE 8.1

**Q. 1** Given  $m\overline{AC} = 1\text{cm}$ ,  $m\overline{BC} = 2\text{cm}$ ,  $m\angle C = 120^\circ$

Compute the length  $AB$  and the area of  $\Delta ABC$ .

Hint :  $(m\overline{AB})^2 = (m\overline{AC})^2 + (m\overline{BC})^2 + 2(m\overline{AC})(m\overline{CD})$

where  $(m\overline{CD}) = (m\overline{BC}) \cos(180^\circ - C)$  (Use theorem I)

**Solution:**

**Given:** In a  $\Delta ABC$   $m\overline{AC} = 1\text{cm}$ ,  $m\overline{BC} = 2\text{cm}$ ,  $m\angle C = 120^\circ$

**To Find:** (i)  $m\overline{AB}$  (ii) Area of  $\Delta ABC$

**Calculations:**

(i) In obtuse angled triangle  $ABC$ , by theorem I

$$(m\overline{AB})^2 = (m\overline{AC})^2 + (m\overline{BC})^2 + 2(m\overline{AC})(m\overline{CD}) \dots\dots\dots (i)$$

In right angled  $\Delta BCD$

$$\cos 60^\circ = \frac{m\overline{CD}}{m\overline{BC}}$$

$$\frac{1}{2} = \frac{m\overline{CD}}{2}$$

$$\overline{CD} = 1\text{cm} \quad \boxed{\overline{CD} = 1\text{cm}}$$

Now putting the corresponding values in (i)

$$\begin{aligned} (m\overline{AB})^2 &= (1\text{cm})^2 + (2\text{cm})^2 + 2(1\text{cm})(1\text{cm}) \\ &= 1\text{cm}^2 + 4\text{cm}^2 + 2\text{cm}^2 \\ &= 7\text{cm}^2 \end{aligned}$$

$$\sqrt{(m\overline{AB})^2} = \sqrt{7\text{cm}^2} \quad \boxed{m\overline{AB} = 2.645\text{ cm}}$$

(ii) Area of  $\Delta ABC = \frac{1}{2} \text{ base} \times \text{Altitude}$

$$\begin{aligned} \text{Area of } \Delta ABC &= \frac{1}{2} m\overline{AC} \times m\overline{BD} \\ &= \frac{1}{2} \times 1\text{cm} \times h \dots\dots\dots (ii) \end{aligned}$$

In right angled triangle  $BCD$

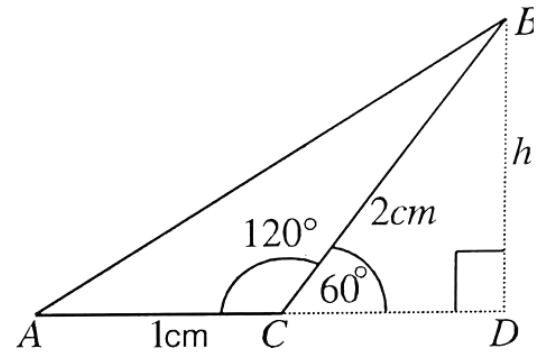
By Pythagoras theorem

$$\begin{aligned} (2\text{cm})^2 &= (1\text{cm})^2 + (h)^2 \\ 4\text{cm}^2 &= 1\text{cm}^2 + h^2 \\ h^2 &= 3\text{cm}^2 \quad h = \sqrt{3}\text{ cm} \end{aligned}$$

Thus equation (ii) becomes

$$\text{Area of } \Delta ABC = \frac{1}{2} \times 1\text{cm} \times \sqrt{3}\text{ cm}$$

$$\text{Area of } \Delta ABC = \frac{\sqrt{3}}{2}\text{cm}^2$$



Q. 2 Find  $m\overline{AC}$  if in  $\triangle ABC$ ,  $m\overline{BC} = 6\text{cm}$ ,  $m\overline{AB} = 4\sqrt{2}\text{cm}$  and  $m\angle ABC = 135^\circ$ .

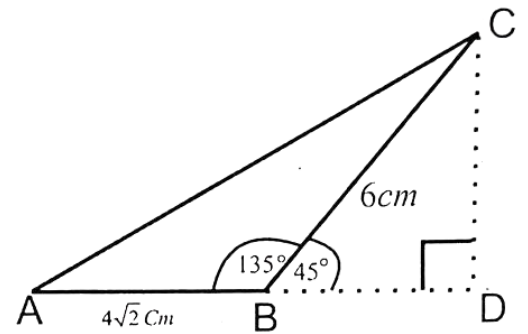
**Solution:**

**Given:**

$$m\overline{BC} = 6\text{cm}$$

$$m\overline{AB} = 4\sqrt{2}\text{cm}$$

$$m\angle ABC = 135^\circ$$



**To Find:**  $m\overline{AC} = ?$

**Calculation:**

In obtuse angled triangle ABC, by theorem 1

$$(m\overline{AC})^2 = (m\overline{AB})^2 + (m\overline{BC})^2 + 2(m\overline{AB})(m\overline{BD}) \dots \dots \dots (i)$$

In right angled  $\triangle BCD$

$$\cos 45^\circ = \frac{m\overline{BD}}{m\overline{BC}}$$

$$\frac{1}{\sqrt{2}} = \frac{m\overline{BD}}{6\text{cm}}$$

$$m\overline{BD} = \frac{6}{\sqrt{2}} \text{ cm}$$

Now putting the corresponding values in equation (i) we get

$$(m\overline{AC})^2 + (4\sqrt{2}\text{ cm})^2 + (6\text{ cm})^2 = 2(4\sqrt{2}\text{ cm}) \frac{6}{\sqrt{2}} \text{ cm}$$

$$= 16(2\text{ cm}^2) + 36\text{ cm}^2 + 8\text{ cm}(6\text{ cm})$$

$$= 32\text{ cm}^2 + 36\text{ cm}^2 + 48\text{ cm}^2$$

$$= 116\text{ cm}^2$$

By taking square root of both sides, we get

$$\sqrt{(m\overline{AC})^2} = \sqrt{116\text{ cm}^2} = \sqrt{4 \times 29\text{ cm}^2}$$

$$m\overline{AC} = 2\sqrt{29}\text{ cm}$$