

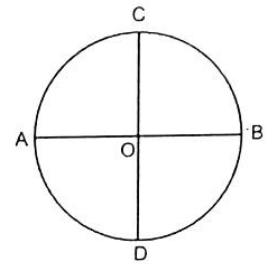
## EXERCISE 9.1

**Q. 1 Prove that, the diameters of a circle bisect each other.**

**Given:** A circle with centre O. Two diameters  $\overline{AB}$  and  $\overline{CD}$ .

**To Prove:** Two diameters  $\overline{AB}$  and  $\overline{CD}$  bisect each other.

**Proof:**



Statements	Reasons
$\overline{AB}$ and $\overline{CD}$ intersect each other at point O. $\overline{OA} \cong \overline{OB}$ ..... (i) O is the midpoint of $\overline{AB}$ thus $\overline{CD}$ bisects the $\overline{AB}$ at O. Similarly $\overline{OC} \cong \overline{OD}$ ..... (ii) O is the midpoint of $\overline{CD}$ thus $\overline{AB}$ bisects the $\overline{CD}$ at O. Hence, two diameters $\overline{AB}$ and $\overline{CD}$ bisect each other.	$\overline{AB}$ and $\overline{CD}$ are non-parallel. Radii of the same circle from (i) Radii of the same circle from (ii)

**Q. 2 Two chords of a circle do not pass through the centre. Prove that they cannot bisect each other.**

**Given:**

A Circle with centre "O". Two different chords  $\overline{AB}$  and  $\overline{CD}$  not passing through the centre, intersect each other at point E.

**To Prove:**

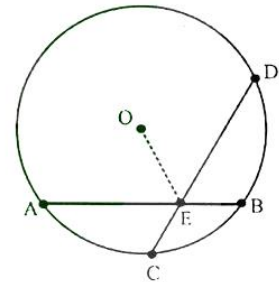
$\overline{AB}$  and  $\overline{CD}$  do not bisect each other, i.e.

E is not midpoint of  $\overline{AB}$  and  $\overline{CD}$ .

**Construction:**

Suppose chords  $\overline{AB}$  and  $\overline{CD}$  bisect each other at point E i.e. E is the common midpoint of  $\overline{AB}$  and  $\overline{CD}$ . Join O to E.

**Proof:**



Statements	Reasons
As $\overline{OE}$ is perpendicular from "O" to the midpoint E of $\overline{AB}$ and $\overline{CD}$ so , $m\angle OEA = 90^\circ$ ..... (i) $m\angle OED = 90^\circ$ ..... (ii) $m\angle OEA + m\angle OED = 180^\circ$ ..... (iii) $m\angle AED = 180^\circ$ It is only possible when A and D are on the same line segment. But A and D are not on the same line segment. So, our supposition, $\overline{AB}$ and $\overline{CD}$ bisect each other, is wrong. Thus chords $\overline{AB}$ and $\overline{CD}$ do not bisect each other	A line segment from the centre "O" to the midpoint of a chord is $\perp$ on the chord. (Construction) Adding (i) and (ii) Given

Q. 3 If length of the chord  $\overline{AB} = 8$  cm. Its distance from the centre is 3 cm, then find the diameter of such circle.

**Solution:**

**Given:**

Length of chord =  $m\overline{AB} = 8$ cm

Distance from centre =  $m\overline{OD} = 3$ cm

**To Find:** Diameter =  $2r$

**Calculations:**

$$m\overline{AB} = 8\text{cm} \quad (\text{Given})$$

Perpendicular from the centre to the chord bisects the chord ( $\overline{OD} \perp \overline{AB}$ )

$$m\overline{AD} = \frac{1}{2} m\overline{AB} = \frac{1}{2} (8\text{cm}) = 4\text{cm}$$

In right angled  $\triangle ADO$  by Pythagoras theorem

$$(m\overline{OA})^2 = (m\overline{AD})^2 + (m\overline{OD})^2$$

$$r^2 = (4\text{cm})^2 + (3\text{cm})^2$$

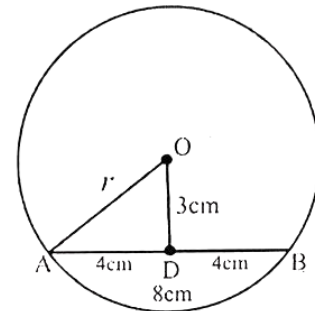
$$r^2 = 16\text{cm}^2 + 9\text{cm}^2$$

$$r^2 = 25\text{cm}^2$$

$$\sqrt{r^2} = \sqrt{25\text{cm}^2}$$

$$r = 5\text{cm}$$

We know that diameter =  $2r = 2(5\text{cm}) = 10\text{cm}$



**Q.4 Calculate the length of a chord which stands at a distance 5cm from the centre of a circle whose radius is 9cm.**

**Given:**

In a circle with centre O radius = 9cm,

$$m\overline{OD} = 5\text{cm}$$

**To find:**

Length of chord  $\overline{AB}$

**Calculations:**

In right angled  $\triangle ADO$ , by Pythagoras theorem

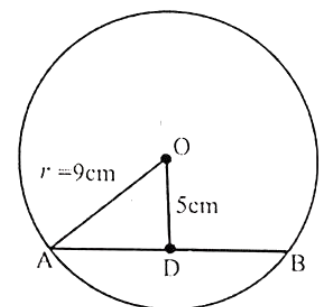
$$(m\overline{OA})^2 = (m\overline{AD})^2 + (m\overline{OD})^2$$

$$(9\text{cm})^2 = (m\overline{AD})^2 + (5\text{cm})^2$$

$$81\text{cm}^2 = (m\overline{AD})^2 + 25\text{cm}^2$$

$$81\text{cm}^2 - 25\text{cm}^2 = (m\overline{AD})^2$$

$$56\text{cm}^2 = (m\overline{AD})^2$$



$$\sqrt{(\overline{mAD})^2} = \sqrt{56\text{cm}^2}$$

$$\overline{mAD} = \sqrt{56\text{cm}}$$

We know that

$$\overline{mAD} = \frac{1}{2} \overline{mAB} \text{ (Perpendicular from the centre to the cord bisects the chord)}$$

$$\Rightarrow \overline{mAB} = 2\overline{mAD}$$
$$= 2 \times \sqrt{56\text{cm}}$$

$$\overline{mAB} = 14.966\text{cm}$$

or  $\overline{mAB} \approx 14.97\text{cm}$